

Closed-Loop Supply Chain Design for Production System using Part and Module

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Abstract. Under the competitive economy environment, reducing the waste of resources and protecting the environment can provide companies with an additional revenue or cost reduction. So many companies concentrate their efforts on the design of closed-loop supply chain (CLSC) model. In previous literatures, many CLSC models were studied, but few of researchers mentioned modular production system and discussed the situation of disassembling of modules and parts together. In this paper, we proposed a new type of CLSC model. The proposed CLSC model considers the production system using part and module in forward logistics and the reselling activities in reverse logistics. For forward logistics, four kinds of part and two kinds of module are used for module manufacturer and product manufacturer, respectively. For reverse logistics, the returned products from customers are classified into two categories which are recoverable and unrecoverable products at recovery center. The recoverable products are resold at used market. The unrecoverable products are disassembled and then classified into recoverable modules, recoverable parts and unrecoverable parts. The recoverable modules and recoverable parts are sent to product manufacturer and module manufacturer. The unrecoverable parts are sent to waste disposal center. The proposed CLSC model is formulated using a nonlinear mixed integer programming and implemented using a hybrid genetic algorithm (HGA) approach. In numerical experiments, various scales of the proposed CLSC problem are presented to compare the performances of the hybrid genetic algorithm with other competing approaches. Experimental results prove that the hybrid genetic algorithm approach outperforms the others.

Keywords: closed-loop supply chain (CLSC), forward and reverse logistics, modular production system, hybrid genetic algorithm (HGA)

1. INTRODUCTION

For meeting internationalization of the market and the

diversity of customer demand, flexibility in manufacturing activities becomes more and more important for manufacturers. A production system using part and module

has been conceived to be very effective in producing product and meeting customer demand. Also, satisfying various environmental legislations is another consideration to manufacturers during their manufacturing activities. Therefore, in order to reduce the waste of resource and protect environment, many manufacturers have been developing various closed - loop supply chain (CLSC) models (Georgiadis *et al.* 2010; Wang *et al.*, 2011; Zhang *et al.* 2011; Chung *et al.* 2011; Hamed *et al.* 2013; Demirel *et al.* 2014; Chen *et al.* 2015).

For the design of the CLSC model, Hamed *et al.* (2013) suggested the CLSC model with three handling processes of returned products, that is, the returned products are sent to secondary market, remanufacturer, and waste disposal center. Chen *et al.* (2015) proposed another type of CLSC model. In the model, they classified returned products into good-quality and poor-quality parts by considering their quality properties.

For production system using module, Wu *et al.* (2011) showed that module production system can increase the product life cycle. Fujita *et al.* (2013) proved that the module production system is able to improve the flexibility and productivity.

For environmental regulation in the CLSC model. Georgiadis *et al.* (2010) performed a case study on the role of recycle products with the waste electrical and electronic equipment (WEEE) in EU.

Many studies related to the CLSC model including the above mentioned studies have been performed using genetic algorithm (GA) approach (Zhang *et al.* 2011; Demirel *et al.* 2014; Chen *et al.* 2015). Zhang *et al.* (2011) studied a CLSC model with capacitated production plan and it was implemented using GA approach. Demirel *et al.* (2014) analyzed the situation of returned product in a CLSC model using GA.

However, although many researchers have studied the CLSC model using GA, GA has some weakness in its search process such as premature convergence or the absence of local search. Therefore, various hybrid GA (HGA) approaches using GA and some local search approaches have been developed (Gen and Cheng 1997, 2000; Lee *et al.* 2002; Yun *et al.* 2013). Recently, Kanagaraj *et al.* (2013) suggested a HGA approach using GA and Cuckoo search (CS). They used Levy flight scheme in CS to improve the search ability in GA.

Based on the above mentioned conventional studies, we propose a new type of the CLSC model using a HGA approach. The proposed CLSC model uses various part and module types for producing product in forward logistics (FL) and reselling activities in reverse logistics (RL). For the HGA approach, we develop an improved HGA (iHGA) approach using the conventional HGA approach by Kanagaraj *et al.* (2013).

In section 2, the proposed CLSC model is represented. The model is designed by a mathematical formulation in section 3. Section 4 shows the procedure of the iHGA approach to implement the mathematical formulation. The iHGA approach including some conventional approaches are applied to the three scales of the CLSC model presented in Section 5. Their performances are compared using various measures. Finally, some conclusions are summarized and the directions for future study are presented in Section 6.

2. STRUCTURE OF CLSC MODEL

Figure 1 shows the structure of the proposed CLSC model.

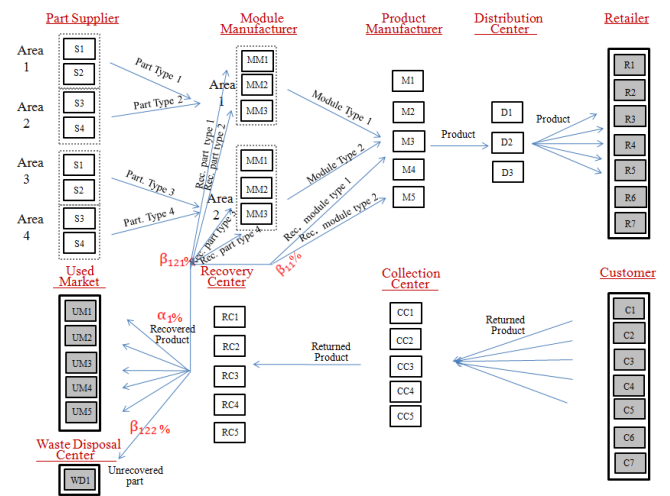


Figure 1: Structure of CLSC model

In Figure 1, the proposed CLSC model has five stages in FL and four stages in RL. For the five stages in FL, part suppliers in four areas, module manufacturers in two areas, product manufacturers, distribution centers and retailers are considered. For the four stages in RL, customers, collection centers, recovery centers, used markets and waste disposal centers are taken into consideration.

For the FL, four types of part are manufactured in part supplier and they are sent to module manufacturer so that two types of module are produced in it. The modules are sent to product manufacturer and then they are assembled for the production of products. Finally, the product are sent to retailer via distribution center.

For the RL, all returned products from customer are sent to recovery center through collection center. At recovery center, all returned products are classified into recoverable products with $\alpha_1\%$ and unrecoverable products with $\beta_1\%$ after testing and checking. The recovered products are resold at used market after some proper recovering process using the recoverable product at recovery center. However, the

unrecoverable products are disassembled into recoverable modules with $\beta_{11}\%$ and unrecoverable modules with $\beta_{12}\%$. The recovered modules are sent to product manufacturer in FL after some proper handling process. The unrecoverable modules are disassembled into recoverable parts with $\beta_{121}\%$ and unrecoverable parts with $\beta_{122}\%$. The recovered parts are sent to module manufacturer after some proper handling process. The unrecoverable parts are sent to waste disposal center. Figure 2 shows the handling processes at recovery center.

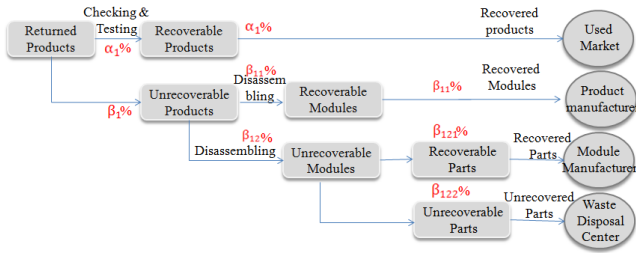


Figure 2: Handling processes at recovery center

3. MATHEMATICAL FORMULATION

In this section, a mathematical formulation is designed for the proposed CLSC model. First, some assumptions are considered as follows.

- Only single item is produced.
- The number of facility at each stage are already known.
- The numbers of retailer, customer, used market and waste disposal center are fixed and all of them are always opened.
- Only one facility at each stage should be opened, except for the stages of retailer, customer, used market and waste disposal center.
- Fixed costs of the facility which will be opened at each stage are different each other and already known.
- Unit handling costs of facilities at each stage are identical and already known.
- Unit transportation cost between each stage are different each other and already known.
- The handling capacity of facilities at a stage is the same or greater than that of facilities at the previous stage.
- The return rate of the returned products from customer is 100%.
- The qualities of recovered modules and parts at recovery center are identical with new ones.

Based on the assumptions mentioned above, a mathematical formulation for the proposed CLSC model is designed. First, index set, parameters, decision variables are defined as follow:

Index Set

- a : index of area of part supplier; $a \in A$
- b : index of area of module manufacturer; $b \in B$
- h : index of part supplier; $h \in H$
- i : index of module manufacturer; $i \in I$
- j : index of product manufacturer; $j \in J$
- k : index of distribution center; $k \in K$
- l : index of retailer/customer; $l \in L$
- m : index of collection center; $m \in M$
- n : index of recovery center; $n \in N$
- o : index of used market; $o \in O$
- p : index of waste disposal center; $p \in P$

Parameters

- $FIXSP_{ha}$: fixed cost of part supplier h at area a
- $FIXMM_{ib}$: fixed cost of module manufacturer i at area b
- $FIXPM_j$: fixed cost of product manufacturer j
- $FIXDC_k$: fixed cost of distribution center k
- $FIXCC_m$: fixed cost of collection center m
- $FIXRM_n$: fixed cost of recovery center n
- $UHSP_{ha}$: unit handling cost of part supplier h at area a
- $UHMM_{ib}$: unit handling cost of module manufacturer i at area b
- $UHPM_j$: unit handling cost of product manufacturer j
- $UHDc_k$: unit handling cost of distribution center k
- $UHCC_m$: unit handling cost of collection center m
- $UHRM_n$: unit handling cost of recovery center n
- $UTSMM_{hai}$: unit transportation cost from part supplier h at area a to module manufacturer i
- $UTMMPM_{ibi}$: unit transportation cost from module manufacturer i at area b to product manufacturer center j
- $UTPMD_{ik}$: unit transportation cost from product manufacturer j to distribution center k
- $UTDR_{kl}$: unit transportation cost from distribution center k to retailer(customer) l
- $UTRCC_{lm}$: unit transportation cost from retailer l to collection center m
- $UTCCRC_{mn}$: unit transportation cost from collection center m to recovery center n
- $UTRCMM_{nib}$: unit transportation cost from recovery center n to module manufacturer i at area b
- $UTRCPM_{ni}$: unit transportation cost from recovery center n to product manufacturer j
- $UTRCWD_{np}$: unit transportation cost from recovery center n to waste disposal center p
- $UTRCSM_{no}$: unit transportation cost from recovery center n to used market o

Decision Variables

- ks_{ha} : handling capacity of part supplier h at area a
- kmm_{ib} : handling capacity of module manufacturer i at area b
- kpm_j : handling capacity of product manufacturer j

kdc_k : handling capacity of distribution center k
 kr_l : handling capacity of retailer l
 kcc_m : handling capacity of collection center m
 krc_n : handling capacity of recovery center n
 ksm_o : handling capacity of used market o
 kwd_p : handling capacity of waste disposal center p

$$\begin{aligned}
y_{sha} &= \begin{cases} 1, & \text{when part supplier } h \text{ at area } a \text{ is opened} \\ 0, & \text{otherwise} \end{cases} \\
y_{mm_{ib}} &= \begin{cases} 1, & \text{when module supplier } i \text{ at area } b \text{ is opened} \\ 0, & \text{otherwise} \end{cases} \\
y_{pm_j} &= \begin{cases} 1, & \text{when product manufacturer } j \text{ is opened} \\ 0, & \text{otherwise} \end{cases} \\
y_{dc_k} &= \begin{cases} 1, & \text{when distribution center } k \text{ is opened} \\ 0, & \text{otherwise} \end{cases} \\
y_{cc_m} &= \begin{cases} 1, & \text{when collection center } m \text{ is opened} \\ 0, & \text{otherwise} \end{cases} \\
y_{rc_n} &= \begin{cases} 1, & \text{when recovery center } n \text{ is opened} \\ 0, & \text{otherwise} \end{cases}
\end{aligned}$$

Objective Functions

$$\begin{aligned}
&\text{Minimize Total Cost (TC)} = \\
&\sum_a \sum_h \text{FIXSP}_{ha} \cdot y_{sha} + \sum_b \sum_i \text{FIXMM}_{ib} \cdot y_{mm_{ib}} + \\
&\sum_j \text{FIXPM}_j \cdot y_{pm_j} + \sum_k \text{DC}_k \cdot y_{dc_k} + \\
&\sum_m \text{FIXCC}_m \cdot y_{cc_m} + \sum_n \text{FIXRC}_n \cdot y_{rc_n} + \\
&\sum_a \sum_h \text{UHSP}_{ha} + \sum_b \sum_i \text{UHMM}_{ib} \cdot kmm_{ib} \cdot y_{mm_{ib}} + \\
&\sum_j \text{UHPM}_j \cdot kpm_j \cdot y_{pm_j} + \sum_k \text{UHDC}_k \cdot kdc_k \cdot y_{dc_k} + \\
&\sum_m \text{UHCC}_m \cdot kcc_m \cdot y_{cc_m} + \sum_n \text{UHRC}_n \cdot krc_n \cdot y_{rc_n} + \\
&\sum_a \sum_h \sum_i \text{UTSMM}_{iha} \cdot ks_{ha} \cdot y_{sha} \cdot kmm_{ib} + \\
&\sum_b \sum_i \sum_j \text{UTMMPM}_{jib} \cdot kmm_{ib} \cdot y_{mm_{ib}} \cdot y_{pm_j} + \\
&\sum_j \sum_k \text{UTPMD}_{kj} \cdot kmm_j \cdot y_{mm_j} \cdot y_{dc_k} + \\
&\sum_k \sum_l \text{UTDR}_{lk} \cdot kdc_k \cdot y_{dc_k} + \\
&\sum_l \sum_m \text{UTRCC}_{ml} \cdot kr_l \cdot y_{cc_m} + \\
&\sum_m \sum_n \text{UTCCRC}_{nm} \cdot kcc_m \cdot y_{cc_m} \cdot y_{rc_n} + \\
&\sum_n \sum_i \sum_b \text{UTRCMM}_{bin} \cdot kmm_{ib} \cdot y_{mm_{ib}} \cdot y_{rc_n} + \\
&\sum_n \sum_j \text{UTRCPM}_{jn} \cdot krc_n \cdot y_{pm_j} + \\
&\sum_n \sum_o \text{UTRCSM}_{on} \cdot ksm_o \cdot y_{rc_n} + \\
&\sum_n \sum_o \text{UTRCWD}_{pn} \cdot kwd_p \cdot y_{rc_n}
\end{aligned} \quad (1)$$

Subject to

$$\sum_h y_{sha} = 1, \forall a \in A \quad (2)$$

$$\sum_i y_{mm_{ib}} = 1, \forall b \in B \quad (3)$$

$$\sum_j y_{pm_j} = 1 \quad (4)$$

$$\sum_k y_{dc_k} = 1 \quad (5)$$

$$\sum_m y_{cc_m} = 1 \quad (6)$$

$$\sum_n y_{rc_n} = 1 \quad (7)$$

$$\sum_h (ks_{ha} y_{sha}) - \sum_i (kmm_i \cdot y_{mm_{ib}}) = 0, \forall a \in A \quad (8)$$

$$\sum_i (kmm_{ib} \cdot y_{mm_{ib}}) - \sum_j (kpm_j \cdot y_{pm_j}) = 0, \forall b \in B \quad (9)$$

$$\sum_i (kpm_j \cdot y_{pm_j}) - \sum_k (kdc_k \cdot y_{dc_k}) = 0 \quad (10)$$

$$\sum_k (kdc_k \cdot y_{dc_k}) - \sum_l kr_l = 0 \quad (11)$$

$$\sum_n (krc_n - \sum_m (kcc_m \cdot y_{cc_m})) = 0 \quad (12)$$

$$\sum_p ksm_o - \alpha_1 \% \sum_n (krc_n \cdot y_{rc_n}) \geq 0 \quad (13)$$

$$\sum_i (kpm_j \cdot y_{pm_j}) - \beta_{11} \% \sum_n (krc_n \cdot y_{rc_n}) \geq 0 \quad (14)$$

$$\sum_i (kmm_{ib} \cdot y_{mm_{ib}}) - \beta_{121} \% \sum_n (krc_n \cdot y_{rc_n}) \geq 0 \quad (15)$$

$$\sum_a (kwd_p - \beta_{122} \% \sum_m (krc_n \cdot y_{rc_n})) \geq 0 \quad (16)$$

$$\sum_n (krc_n \cdot y_{dc_k}) - \sum_o ksm_o = 0 \quad (17)$$

$$y_{sha} = \{0,1\}, \forall h \in H, a \in A \quad (18)$$

$$y_{mm_{ib}} = \{0,1\}, \forall i \in I, b \in B \quad (19)$$

$$y_{pm_j} = \{0,1\}, \forall j \in J \quad (20)$$

$$y_{dc_k} = \{0,1\}, \forall k \in K \quad (21)$$

$$y_{cc_m} = \{0,1\}, \forall m \in M \quad (22)$$

$$y_{rc_n} = \{0,1\}, \forall n \in N \quad (23)$$

$$\begin{aligned}
&ks_{ha}, kmm_{ib}, kpm_j, kdc_k, kcc_m, krc_n, ksm_o, kwd_p \geq 0, \\
&\forall h \in H, a \in A, \forall i \in I, b \in B, j \in J, \forall k \in K, \forall l \in L, \forall m \in M, \forall n \in N, \\
&\forall o \in O, \forall p \in P
\end{aligned} \quad (24)$$

The above mathematical formulation is a nonlinear mixed integer programming. The equation (1) shows the objective function which total cost should be minimized. The total cost is consist of the sum of fixed costs, handling costs and transformation costs resulting from each stage. From equation (2) to (7) represent that only one facility at each stage can be opened. Equation (8) means that the each sum of parts at all part suppliers of areas 1, 2, 3, and 4 is the same as that of the modules at all module manufacturer of areas 1 and 2. Equation (9) to (12) have the same meaning with equation (8). Equation (13) to (17) restrict that the sum of the handling capability at each stage is the same or greater than that at the previous stage. From equation (18) to (23) shows that all facilities at each stage have 1 (opening) or 0 (closing). Equation (24) restricts that all variables have non negativity value.

4. PROPOSED METHODOLOGY

As shown in Section 1, GA has been proved to be very effective in locating global optimal solution to many CLSC models (Chen *et al.* 2015). Unfortunately, however, GA has some weakness such as premature convergence and the absence of local search. Therefore, various HGAs have been developed.

Recently, Kanagaraj *et al.* (2013) proposed a new type of HGA using GA and CS. They used Levy flight concept in CS in order to produce respective offspring in GA. The main logic of the HGA is to apply Levy flight scheme to a new individual from the population after GA search process. If the fitness value of the new individual is superior to that of the individual randomly selected from the population, then the new individual is included into the offspring for next generation. However, this process is done by only one time at every generation. Therefore, a weakness in this process may be happened, that is, if the fitness value of the new individual does not be superior to that of the individual randomly selected from the population, then the new

individual is not included into the offspring for next generation.

For overcome this weakness of the search process of the HGA by Kanagaraj *et al.* (2013), the iHGA is proposed here. In the iHGA, Levy flight scheme is adapted to all individuals from the population after GA search process, which can increase the occurrence possibility of respective individuals of GA. The detailed implementation procedure is shown in Figure 3.

```

procedure iHGA approach
input problem data, parameters
begin
  Randomly generate initial parent population;
  while (not termination condition) do
    Create offspring population by two-point crossover
    operator and one-point mutation operator;
    for  $i = 1$  to population size
      Select a new individual ( $new_i$ ) from offspring
      population;
      Apply Levy flight to  $new_i$ ;
      Randomly select a new individual ( $old_i$ ) from
      offspring population;
      if  $f(new_i) \geq f(old_i)$  then
        Insert  $new_i$  into Offspring population;
      end
    end
    Sorting all individuals of offspring;
    A fraction ( $p_a$ ) of worst individuals in offspring are
    abandoned;
    Regenerate new individuals randomly to replace the
    lost individuals;
  end
output a best solution;
end;

```

Figure 3: Implementation procedure of iHGA

5. NUMERICAL EXPERIMENT

In numerical experiment, three scales of the proposed CLSC model are presented as shown in Table 1. Each scale

has various numbers of facilities. As mentioned in assumption of Section 3, all facilities at retailer/customer (R), used market (UM) and waste disposal center (WD) are always opened. However, only one facility at part supplier (PS), module manufacturer (MM), product manufacturer (PM), distribution center (DC), collection center (CC), recovery center (RC) should be opened.

For each scale, the iHGA, the HGA by Kanagaraj *et al.* (2013), the GA by Gen and Cheng (1997) and Lingo by Lindo Systems (2015) are adapted. All approaches were run on IBM compatible PC3.4HGZ processor (Inter Core i7-3770 CPU), 8GB RAM and Window 7. The iHGA, HGA and GA except for Lingo were programmed using MATLAB 2015a.

In parameter setting, population size is 20, crossover rate is 0.5, mutation rate is 0.3, and total number of generation is 10,000. All approaches were run 30 trials for eliminate a randomness in their search processes. For various comparisons among all approaches, five measures of performance as shown in Table 2 are used.

Table 3 shows computation result for scale 1, 2 and 3. For scale 1, in terms of the best solution, the Lingo shows the best result and the GA has the worst one. The iHGA slightly outperforms the HGA. Similar results are also shown in terms of the average solution. In terms of the average iteration, the performance of the GA is the worst and that of the HGA is the best. The average search time to the pre-defined total number of generations shows the iHGA is the slowest and the HGA is the quickest.

For scale 2, in terms of the best solution, average solution and average iteration, the performances of the iHGA are superior to those of the others except for the Lingo. However, the search speed of the iHGA is almost three times slower than those of the GA and HGA. For scale 3, in terms of the best solution, the Lingo shows the best result, but in the comparison of the others, the performance of the iHGA is slightly better than those of the GA and HGA. A similar result is also shown in terms of the average solution, that is, the iHGA outperforms the GA and HGA. However, in terms of the average time, the search speed of the iHGA is significantly slower than those of the others.

Table 2: Measure of performance

Measure	Description
Best solution	The best value among the objective functions under satisfying all constraints.
Average solution	Averaged value of the objective functions under satisfying all constraints.
Average iteration	Averaged number of iteration after all trials.
Best setting	Opened number PS, MM, PM, DC, CC and RC when the best solution is obtained.
Average time	Average running time (in Sec.) after all trials.

Table 1: Three types of CLSC model

Scale	No. of PS	No. of MM	No. of PM	No. of DC	No. of R	No. of CC	No. of RC	No. of UM	No. of WD
	Area 1,2,3,4	Area 1,2							
1	8	8	12	8	20	12	8	20	4
2	10	10	14	10	25	14	10	25	5
3	20	20	28	20	50	20	20	50	10

Table 4 show the location decision result of GA, HGA, and iHGA for scale 3.

product manufacturer, 2,000 modules (=1,000 module 1 + 1,000 module scale 2) at module manufacturer of each area are required. Also, for producing 2,000 module at module

Table 3: Computation results of scale 1, 2 and 3

	Scale 1				Scale 2				Scale 3			
	GA	HGA	iHGA	Lingo	GA	HGA	iHGA	Lingo	GA	HGA	iHGA	Lingo
Best Solution	138,460	138,253	138,177	136,305	138,869	138,952	138,724	136,112	142,711	142,579	142,450	133,443
Average Iteration	5,547	3,941	4,789	-	5,832	5,267	4,469	-	4,986	4,754	4,946	-
Average Solution	139,081	139,039	139,006	-	139,839	139,866	139,763	-	143,337	143,368	143,244	-
Average Time	12.10	10.14	32.74	-	22.93	23.88	58.30	-	17.37	19.67	58.27	-

Table 4: Location decision result of GA, HGA and iHGA for scale 3

	Best Solution	Area 1	Area 2	Area 3	Area 4	PS		MM		PM		DC		CC		RC	
						No.	No.	No.	No.	No.	No.	No.	No.	No.	No.		
GA	142,711	4	13	18	18	5	5	19	10	17	16						
HGA	142,579	2	19	16	10	10	6	25	14	4	14						
iHGA	142,450	18	3	9	14	20	3	11	13	3	9						

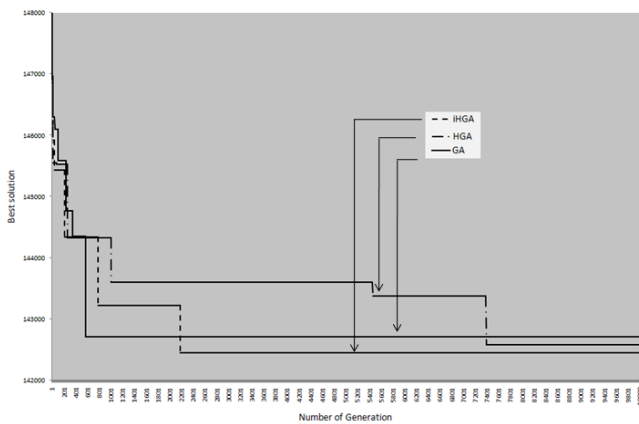


Figure 4: Convergence behaviors of GA, HGA and iHGA

Figure 4 shows that the convergence behaviors of GA, HGA, and iHGA for scale 3. The GA, HGA and iHGA are rapidly converging until about 103, 265 and 223 generations, respectively. After that, they all have slow convergence processes. This convergence behaviors implies that the search scheme used in the iHGA is more efficient than those of the GA and HGA.

Figure 5 shows the location decision result using the CLSL model for scale 3. We suppose that there are 1,000 products to be produced. For producing 1,000 product at

manufacturer at each area, 4,000 parts (=1,000 part type 1 +1,000 part type 2 + 1,000 part type 3+ 1,000 part type 4) at part supplier of each area are required.

The 1,000 product at product manufacturer are then sent to all retailers through distribution center. The 1,000 returned products are sent to recovery center from customer and collection center. Of 1,000 returned products, 700 (=1,000 * 70%) recovered products are sent and resold at used market. 300(=1,000*30%) unrecovered products are disassembled into 300 (150=300*15% for module type 1, 150=300*15% for module type 2) recoverable modules and 300 (150=1000*15% for module type 1, 150=1000*15% for module type 2) unrecoverable modules. The 300 unrecoverable modules are also disassembled into 400(100 = 1000*10% for part type 1, 100 = 1000*10% for part type 2, 100 = 1000*10% for part type 3, 100 = 1000*10% for part type 4) recoverable parts, and 200 (50 = 1000*5% for part type 1, 50 = 1000*5% for part type 2, 50 = 1000*5% for part type 3, 50 = 1000*5% for part type 4) unrecoverable parts.

Based on the analyses using scale 1, 2, and 3, we can summarize the following some conclusions.

In terms of the best and average solutions, although the Lingo used in a benchmark shows the best results, the performances of the iHGA is superior to those of the GA and HGA, which implies that the search scheme used in the iHGA is more efficient in locating best solution than those in the GA and HGA, since the iHGA uses a improve levy flight scheme

rather than the HGA does and the GA does not use any hybrid scheme.

- In terms of the average time, the search speeds of the HGA is significantly quicker than that of the iHGA. This means that HGA uses Levy flight only one time at every generation, but the iHGA uses Levy flight as many as population size at every generation. Therefore, the former is able to search all possible search spaces more quickly than the latter.

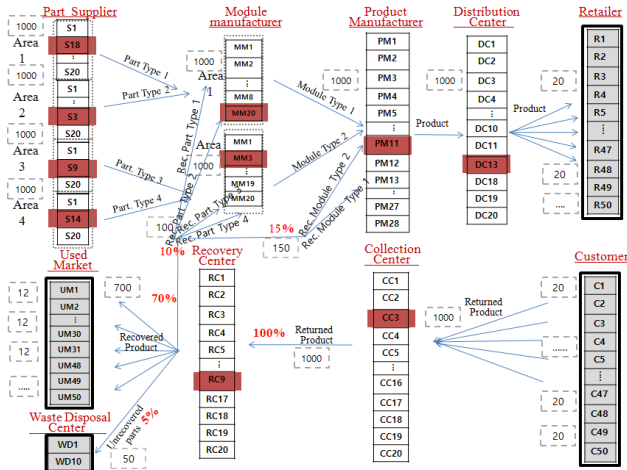


Figure 5: Location decision result using CLSC network for scale 3

6. CONCLUSIONS

In this paper, the CLSC model including forward and reverse logistics has been studied. Many researchers have suggested various types of the CLSL model. However, few of them focused on the production activity using part and module and the resell activities at used market. Therefore, this paper have proposed a new type of the CLSC model both with the production activity using part and module and with the resell activities at used market.

The proposed CLSC model have considered part suppliers and module manufacturer at various areas, product manufacturer, distribution center and retailer in forward logistics and customer, collection center, recovery center, used market and waste disposal center in reverse logistics. For representing the proposed CLSC model, a mathematical formulation is designed and it is implemented in iHGA approach. The iHGA approach is a revised version of the HGA Kanagaraj *et al.* (2013).

In numerical experiments, three scales of the CLSC model have been presented for comparing the performances of the iHGA, HGA and GA approaches under various measures of performance. The experiment results have shown the following two points. Firstly, the performances of the iHGA are more efficient in locating best solution and

average solution than those of the GA and HGA. Secondly, in terms of the search speed, the iHGA does not be efficient than the GA and HGA. Therefore, an effort to reduce the search speed will be required for the iHGA and larger-sized CLSC model will be presented to compare the performance of the iHGA with those of the others. Also, various hybrid approaches using GA and other local search such as particle swarm optimization, ant colony optimization and so on will be proposed.

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